

Grade 8 TEKS Companion Guide

A review guide for the Grade 8 Mathematics Texas Essential Knowledge and Skills
Student Edition

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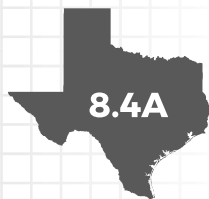
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Printed in the United States of America.

ISBN 978-1-948709-01-9

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SLOPE AS A RATE OF CHANGE



The student is expected to use similar right triangles to develop an understanding that slope, m , given as the rate comparing the change in y -values to the change in x -values, $\frac{y_2 - y_1}{x_2 - x_1}$, is the same for any two points (x_1, y_1) and (x_2, y_2) on the same line.

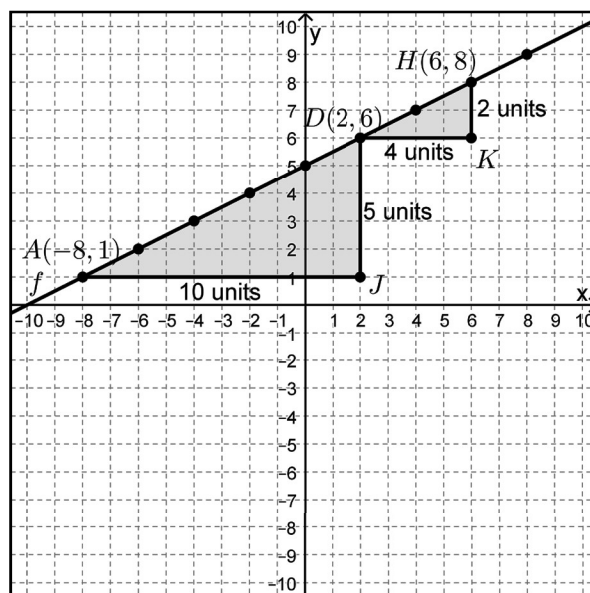


TELL ME MORE...

The slope of a line is a measure of the steepness of its graph. In the graph shown, line f has a slope of $\frac{1}{2}$, meaning that the ratio of the change in the vertical direction to the change in the horizontal direction is $\frac{1}{2}$.

Consider three points along line f : $A(-8, 1)$, $D(2, 6)$, and $H(6, 8)$. Let \overline{AD} be the hypotenuse of right triangle AJD and \overline{DH} be the hypotenuse of right triangle DKH as shown in the graph.

- The vertical distance between points A and D is represented by \overline{JD} , which has a length equal to the difference of the y -coordinates of D and A : $6 - 1 = 5$.
- The horizontal distance between points A and D is represented by \overline{AJ} , which has a length equal to the difference of the x -coordinates of D and A : $2 - (-8) = 10$.
- The vertical distance between points D and H is represented by \overline{KH} , which has a length equal to the difference of the y -coordinates of H and D : $8 - 6 = 2$.
- The horizontal distance between points D and H is represented by \overline{DK} , which has a length equal to the difference of the x -coordinates of H and D : $6 - 2 = 4$.



Triangles AJD and DKH are similar, so the ratios of corresponding side lengths are equal.

$$\begin{aligned}\frac{JD}{AJ} &= \frac{KH}{DK} \\ \frac{6-1}{2-(-8)} &= \frac{8-6}{6-2} \\ \frac{5}{10} &= \frac{2}{4}\end{aligned}$$

The equivalent ratios represent the slope of line f . For any two points on line f , (x_1, y_1) and (x_2, y_2) , the slope of line f is the ratio of the vertical distance ($y_2 - y_1$) to the horizontal distance ($x_2 - x_1$) between the two points.



EXAMPLES

EXAMPLE 1: Triangles ABC and DEF are similar right triangles. Write a proportion that could be used to show that the slope of \overline{DF} is the same as the slope of \overline{AC} .

STEP 1 Identify the coordinates of points A , C , D , and F .

A $(-7, 9)$

C $(0, -5)$

D $(-4, 3)$

F $(-1, -3)$

STEP 2 Use the coordinates of D and F to write the slope of \overline{DF} as the ratio of the vertical distance to the horizontal distance. Let $D(-4, 3) = (x_1, y_1)$ and $F(-1, -3) = (x_2, y_2)$.

$$\frac{\text{vertical distance}}{\text{horizontal distance}} = \frac{y_2 - y_1}{x_2 - x_1} = \frac{-3 - 3}{-1 - (-4)}$$

$$\text{Slope of } \overline{DF} = \frac{-3 - 3}{-1 - (-4)}$$

STEP 3 Use the coordinates of A and C to write the slope of \overline{AC} as the ratio of the vertical distance to the horizontal distance. Let $A(-7, 9) = (x_1, y_1)$ and $C(0, -5) = (x_2, y_2)$.

$$\frac{\text{vertical distance}}{\text{horizontal distance}} = \frac{y_2 - y_1}{x_2 - x_1} = \frac{-5 - 9}{0 - (-7)}$$

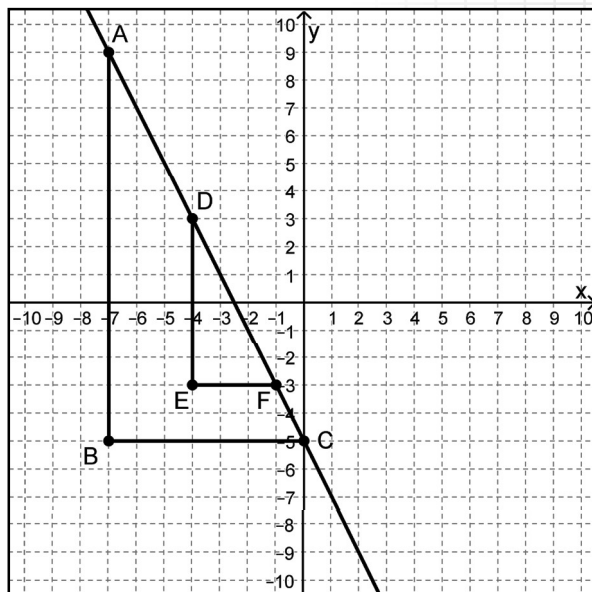
$$\text{Slope of } \overline{AC} = \frac{-5 - 9}{0 - (-7)}$$

STEP 4 A proportion is two or more equivalent ratios. Write a proportion setting the ratios for each slope equal to each other.

$$\text{Slope of } \overline{DF} = \text{Slope of } \overline{AC}$$

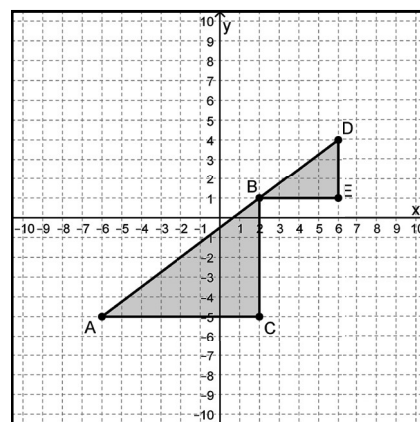
$$\frac{-3 - 3}{-1 - (-4)} = \frac{-5 - 9}{0 - (-7)}$$

$$\frac{-6}{3} = \frac{-14}{7}$$



YOU TRY IT!

Triangle ABC and BDE are similar right triangles. Write a proportion using the coordinates of points A , B , and D to show that the slope of \overline{AB} is equal to the slope of \overline{BD} .



$$\text{Slope of } \overline{AB} = \text{Slope of } \overline{BD}$$

$$\frac{\square - \square}{\square - \square} = \frac{\square - \square}{\square - \square}$$

EXAMPLE 2: The table contains some points contained on line k . Triangle FGM is similar to triangle HJN . Write a proportion to show that the slope of \overline{FG} is equal to the slope of \overline{HJ} .

	x	y
F	-8	6
G	-4	5
H	4	3
J	8	2

STEP 1 Use the coordinates of F and G to write the slope of \overline{FG} as the ratio of the vertical distance to the horizontal distance. Let $F(-8, 6) = (x_1, y_1)$ and $G(-4, 5) = (x_2, y_2)$.

$$\frac{\text{vertical distance}}{\text{horizontal distance}} = \frac{y_2 - y_1}{x_2 - x_1} = \frac{5 - 6}{-4 - (-8)}$$

$$\text{Slope of } \overline{FG} = \frac{5 - 6}{-4 - (-8)}$$

STEP 2 Use the coordinates of H and J to write the slope of \overline{HJ} as the ratio of the vertical distance to the horizontal distance. Let $H(4, 3) = (x_1, y_1)$ and $J(8, 2) = (x_2, y_2)$.

$$\frac{\text{vertical distance}}{\text{horizontal distance}} = \frac{y_2 - y_1}{x_2 - x_1} = \frac{2 - 3}{8 - 4}$$

$$\text{Slope of } \overline{HJ} = \frac{2 - 3}{8 - 4}$$

STEP 3 A proportion is two or more equivalent ratios. Write a proportion setting the ratios for each slope equal to each other.

$$\text{Slope of } \overline{FG} = \text{Slope of } \overline{HJ}$$

$$\frac{5 - 6}{-4 - (-8)} = \frac{2 - 3}{8 - 4}$$

$$\frac{-1}{4} = \frac{-1}{4}$$

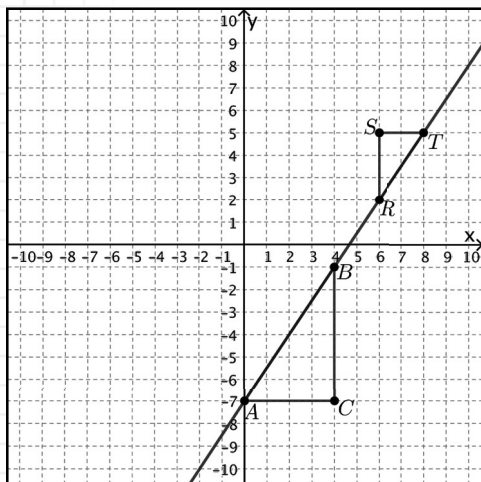
MAKE A NOTE ...

Suppose that $M(4, 8)$ and $N(-2, 5)$. How does the slope of \overline{MN} compare to the slope of \overline{NM} ?



PRACTICE

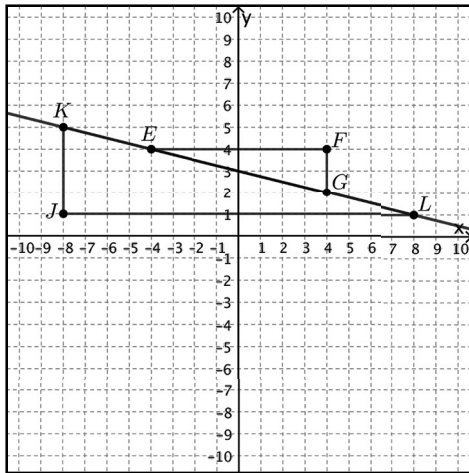
Use the graph to answer questions 1 – 3.



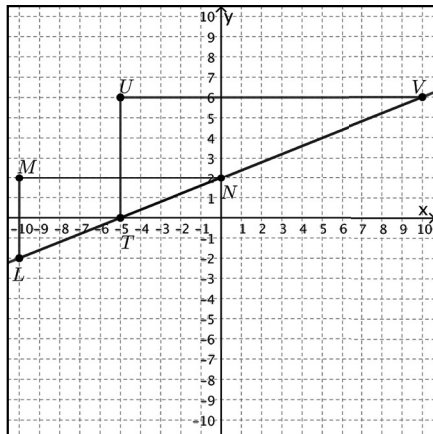
- Write a ratio to show the slope of \overline{AB} .
- Write a ratio to show the slope of \overline{RT} .
- Complete the following statement using an inequality or equality symbol.

$$\text{Slope of } \overline{AB} \text{ _____ Slope of } \overline{RT}$$

Use the graph to answer questions 4 – 6.

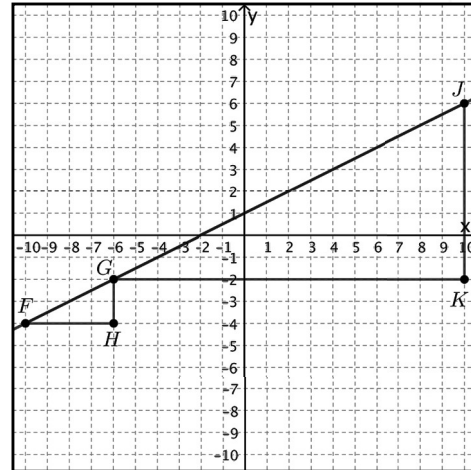


4. What ratio represents the slope of the hypotenuse of triangle JKL ?
5. What ratio represents the slope of the hypotenuse of triangle EFG ?
6. What is the relationship between the two slope values?
7. Triangles LMN and TUV are similar right triangles. Which proportion shows that the slope of LN and the slope of \overline{TV} are equal?

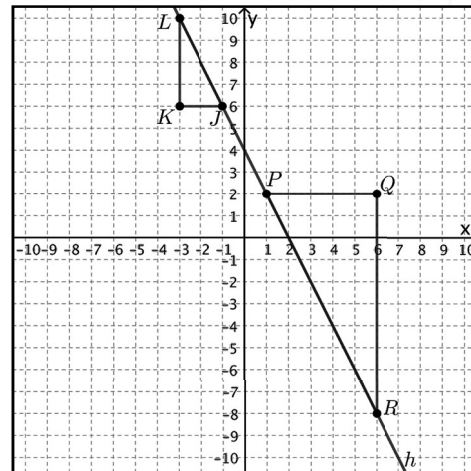


- A $\frac{-2-2}{-10-0} = \frac{0-6}{-5-10}$
- B $\frac{-10-2}{-2-0} = \frac{-5-6}{0-10}$
- C $\frac{-10-0}{-2-2} = \frac{-5-10}{0-6}$
- D $\frac{-2-0}{-10-2} = \frac{0-10}{-5-0}$

8. Triangle FGH and GJK are similar right triangles. Write a proportion using the coordinates of F , G , and J to show that the slopes of \overline{FG} and \overline{GJ} are equal.



9. Triangles KJL and PQR are similar right triangles plotted along line h .



Which statement is true?

- F The slope of the hypotenuse of JKL is less than the slope of the hypotenuse of PQR .
- G The slope of the hypotenuse of JKL is the same as the slope of the hypotenuse of PQR .
- H The slope of the hypotenuse of JKL is greater than the slope of the hypotenuse of PQR .
- J The slopes of the hypotenuses of JKL and PQR have no relationship.